The basic paradigm used by financial economists to explain rates of return on assets was called into question a few years ago by economists Rajnish Mehra of the University of California at Santa Barbara and Edward Prescott of the University of Minnesota. In a 1985 article published in the Journal of Monetary Economics, Mehra and Prescott presented a powerful argument that commonly used economic models were incapable of accounting for the historically observed rates of return on stocks and short-term bonds (bills). Specifically, they found that, in the 90 years from 1889 to 1978, the average real rate of return on stocks was 6.98 percent per year, while the average real rate of return on bills was only 0.80 percent per year. The rate of return on stocks minus the rate of return on bills—the so-called equity premium—averaged an astonishing 6.18 percent per year.

Why was the equity premium so large? The
obvious answer is "risk." Stocks are much riskier than bills, and investors would not want to hold stocks unless they were compensated for the higher risk by earning a higher average rate of return. This basic insight—that investments with higher risk should earn higher average returns—underlies the capital asset pricing model (CAPM), initially developed in the 1960s and refined considerably in the last three decades.

Perhaps the most significant refinement, the consumption capital asset pricing model (CCAPM), recognizes that the ultimate reason for holding wealth is to provide for future consumption; as a result, the equity premium should depend on the variability of consumption and its relation to stock returns. In light of the small fluctuations in U.S. real consumption per capita, however, Mehra and Prescott found that the CCAPM could account for an equity premium of only 0.35 percent per year, a tiny fraction of the historically observed equity premium. To describe this large discrepancy, they coined the term "equity premium puzzle."

Trying to explain average rates of return over a historical time period is a much less formidable task than, say, trying to forecast the returns on stocks or bills in any particular year. Indeed, economists readily admit their limited ability to forecast asset returns. But the CCAPM’s inability to account for average rates of return on stocks and bills, even after the fact, is a serious indictment of this model’s practical value.

Moreover, the basic CCAPM is essentially the same as the model underlying the theory of long-run economic growth and the new strand of classical macroeconomics known as real-business-cycle theory. If the CCAPM has to be discarded or even drastically altered, then much of growth theory and new classical macroeconomics may need a major overhaul. Indeed, the equity premium puzzle could lead economists to reformulate basic models of decisionmaking in the presence of risk.

THE CONSUMPTION CAPITAL ASSET PRICING MODEL

The CCAPM is a sophisticated economic model of the prices and rates of return on assets. To understand its basic workings, let’s first see how asset prices would be determined if investors did not care about the riskiness of their investments.

Risk-Neutral Investors. Confronted with two assets offering different expected rates of return, risk-neutral investors would buy the asset with the higher expected rate of return and sell the asset with the lower expected rate of return. These purchases and sales by investors, however, ultimately affect the expected rates of return. The asset with the higher expected rate of return would attract buyers, and its price would be bid upward. Of course, when the price of the asset increases, its rate of return falls because investors must pay more to receive its payoffs. Similarly, the asset with the lower expected rate of return would fall in price as investors sold it. The fall in price would increase the asset’s expected rate of return by allowing investors to acquire ownership and future payoffs at a lower price.

The adjustment of asset prices and rates of return would cause the gap between the rates of return to shrink. When there is no more upward or downward pressure on asset prices, the asset markets are said to be in equilibrium, and the expected rates of return on both assets will be the same. Thus, with risk-neutral investors, the basic model of asset pricing predicts that asset prices will adjust until all assets offer equal expected rates of return.

Risk-Averse Investors. Most investors are anything but risk-neutral, demanding a higher expected rate of return in order to hold a riskier asset. But how do we measure the riskiness of an asset? The CCAPM offers a very precise answer. Instead of measuring the riskiness of an asset simply by the variability of its returns, the CCAPM uses the relationship between the asset’s returns and the value an investor places
on having an additional dollar of funds. When the investor's overall wealth is low, his consumption is low and he places a relatively high value on an additional dollar of funds. And when the investor's overall wealth is relatively high, his consumption is relatively high and the value he places on an additional dollar of funds is relatively low.

According to the CAPM, an asset is risky if its low payoffs occur when consumption is low (and the value of additional funds is high), and its high payoffs occur when consumption is high (and the value of additional funds is low). On the other hand, an asset would have negative risk if its high returns occur when consumption is low and its low returns occur when consumption is high; in this case, rather than being risky, the asset would provide insurance by offering high returns when the investor values additional funds most highly (when consumption is low).

The CAPM predicts that risk-averse investors will choose assets with the highest expected value of returns weighted by the value placed by investors on additional funds. As in the case of risk-neutral investors, prices will adjust until equilibrium is reached. In equilibrium, the expected rates of return weighted by the value of additional funds will be the same for all assets. Nevertheless, assets with relatively high risk will have higher average returns than assets with relatively low risk. The higher average return of a risky asset is offset by the fact that the high returns occur when additional funds have low value to investors.

If we apply the CAPM to stocks and bills, the average rates of return weighted by investors' value of additional funds should be equal for stocks and bills. To the extent that stock returns (which comprise dividends plus capital gains or losses resulting from changes in the prices of stocks) are riskier than bill returns, the average rate of return on stocks should be higher than the average rate of return on bills. How much higher depends quantitatively on two factors: (1) the covariances of consumption growth with stock returns and bill returns, which measure the sizes of fluctuations in returns and how strongly these fluctuations are related to the fluctuations in consumption growth; and (2) the coefficient of relative risk aversion, A, which indicates how much the value of additional funds increases when consumption falls.4

Mehra and Prescott combined a simple economic model conventionally used in growth theory and real-business-cycle theory with the actual historical variability of U.S. consumption to capture the covariances of consumption with asset returns. The value of A is an important ingredient in this analysis, and, based on their reading of theoretical and empirical research, Mehra and Prescott argued that conventionally accepted values for A lie between 0 and 10. Using a variety of values for A in this range, they found that, in the framework of the

1The value of additional funds is measured by what economists call "the marginal utility of consumption."

2Equilibrium is represented by the following technical condition: E[1 + r1] * MU1 = E[1 + r2] * MU2, where MU is the marginal utility of consumption (the value of additional funds), r1 and r2 are the real rates of return on assets 1 and 2, respectively, and E[ ] denotes the expectation of the term that appears inside the brackets.

3Technically, the covariance of stock returns with consumption growth equals the product of the correlation coefficient between stock returns and consumption growth, the standard deviation of stock returns, and the standard deviation of consumption growth.

4If the coefficient of relative risk aversion equals A, then a 1 percent fall in consumption increases the value in which an investor places an additional dollar of funds by A percent. For example, if A = 6, then a 2 percent fall in consumption increases the value of an additional dollar of funds by 12 percent.
CCAPM, they could not simultaneously account for an average equity premium higher than 0.35 percent per year and an average return on bills of less than 4 percent per year. For the average equity premium to be as large as the historically observed equity premium, the value of A would have to be extremely high, around 30 or 40, which is much higher than the conventionally accepted values for A.

To see why values of A around 30 or 40 are conventionally viewed as implausibly high, suppose that you face a risky situation that will either raise your total wealth by 50 percent or lower it by 50 percent, and each of these outcomes has a 50-50 chance of occurring. How much would you be willing to pay for insurance to avoid this risky situation? If you were risk-neutral, so that A = 0, you would not care about risk and would pay zero for such insurance. However, if risk-averse, you would be willing to pay something for this insurance, and the amount would depend on the strength of your risk aversion measured by A. With A = 2, you would be willing to pay 25 percent of your wealth; with A = 10, you would be willing to pay 46 percent; and with A = 30, you would be willing to pay 49 percent. Because it seems implausible that you would pay 49 percent of your wealth to avoid an even chance of losing 50 percent of your wealth or gaining 50 percent of your wealth, many economists reject as implausible values of A as high as 30.

In addition to financial assets, total wealth includes all other tangible assets, such as real estate and consumer durables, and also human capital, which is the present value of a person's current and future labor income.

The general formula is

\[
y = 1 - \left[1 - \left( \frac{1}{2} \right) \left( 1 - x \right)^{A} + \left( \frac{1}{2} \right) \left( 1 + x \right)^{1/A} \right],
\]

where x is the fraction of your wealth that you could gain or lose with a 50-50 chance, A is the coefficient of relative risk aversion, and y is the fraction of your wealth that you would pay to avoid this risk.

**REEXAMINATION OF THE DATA**

One approach to reconciling the gap between the CCAPM and the average actual equity premium reported by Mehran and Prescott is to reexamine the historical data. Ten average rates of return on bills (0.80 percent per year) and stocks (6.98 percent per year) reported by Mehran and Prescott are based on 90 years of U.S. data. However, recent research by Jeremy Siegel (1991) indicates that the rates of return in the years between 1889 and 1978 may not have been truly representative of the underlying rates of return over a longer span of time. Siegel compiled annual rates of return on stocks and bills for the period from 1802 to 1990, starting 87 years before and ending 12 years after the period examined by Mehran and Prescott. The variability of stock returns is much greater than the variability of bill returns, which is consistent with the notion that stocks are much riskier than bills.

Although the greater variability of stock returns is clear from Figure 1, the difference in the average rates of return on stocks and bills is not. To get a clearer view of the average rates of return, we can calculate the 30-year moving average rate of return, which, for any given year, is the average of the rates of return over the previous 30 years. In Figure 2, the difference between the 30-year moving averages of returns for stocks and for bills is the average of the equity premium over the previous 30 years. The 30-year moving average equity premium increased substantially during the 1940s and 1950s and remained high during the 1960s and 1970s.

The average rates of return calculated by Siegel for the period examined by Mehran and Prescott (1889-1978) differ somewhat from the values reported by Mehran and Prescott (see...
The differences arise because Siegel used a different stock price index, a different measure of inflation, and, for part of the period, a different short-term interest rate. Despite these differences, the basic result is the same: the average equity premium from 1889 to 1978 was very large—well over 6 percent per year. But including the additional 99 years of data in Siegel's study reduces the average equity premium from 6.96 percent per year to 4.62 percent per year. The reason for this drop is that the average real rate of return on bills rises to 3.19 percent per year when we include data over the entire 1802-1990 period; the average real rate of return on stocks is virtually the same over that period as over the period studied by Mehra and Prescott. However, even this lower value of the equity premium is much higher than that predicted by the CAPM examined by Mehra and Prescott. 8

Another way to examine the reliability of the historical average rates of return is to estimate how close the historical average rates of return are to the underlying rates of return investors expect when making their portfolio decisions. Applying statistical techniques to data from 1892 to 1988, Stephen Cecchetti, Pok-sang Lam, and Nelson Mark (1991) found that the average equity premium was 6.03 percent, but that the equity premium expected by investors could have been anywhere from 2.35 percent to 9.71 percent. 9 Even the low value of 2.35 percent for the equity premium is higher than the CAPM studied by Mehra and Prescott can explain. Because the equity premium still appears large after reexamining the historical data on returns, the next step is to reexamine the basic CAPM.

EXTENSIONS OF THE BASIC CAPM

The other approach to explaining the equity premium puzzle is to see if the basic CAPM can be modified to produce a realistic value of 10.

9More precisely, their statistical analysis indicates that if the expected equity premium was constant, then we can be 95 percent confident that it was in the range of 2.35 percent to 4.71 percent. As for the riskless rate, its average value was 3.13 percent, and we can be 95 percent confident that the expected value of the riskless rate was between -0.47 percent and 2.77 percent.
the average equity premium using a value of the coefficient of relative risk aversion, $\lambda$, in the conventionally accepted range of 0 to 10. Several potential modifications are discussed below.

**Other Models of Underlying Risk.** In their version of the CCAPM, Mehra and Prescott assumed that consumption fluctuations behaved according to a simple model that does not allow for the possibility of a large, sudden drop in consumption as might occur during a sharp depression. In addition, Mehra and Prescott assumed that fluctuations in stock dividends were matched exactly by fluctuations in consumption, and they used historical data on consumption to measure the variability of dividends. Subsequent research, discussed below, has studied the importance of these assumptions by allowing for large, sudden drops in consumption and by allowing fluctuations in dividends to differ from fluctuations in consumption.

In a recent study, Thomas Reitz (1988) argued that if there is some possibility of a large, sudden drop in consumption accompanied by a large, sudden drop in dividends, then investors would be willing to hold stocks only if compensated by a high average equity premium. He found that extending the CCAPM to include the possibility of depressions with large, sudden drops in consumption could account for the historically observed equity premium. However, Mehra and Prescott (1988) point out that the potential depressions analyzed by Reitz involved declines in consumption of 25 percent or more during a single year. While it is true that consumption during the Great Depression fell 22 percent between 1929 and 1933, Mehra and Prescott point out that in no single year did consumption fall as much as 9 percent. Thus, they conclude that the drops in consumption in Reitz’s study are too large to provide a realistic solution to the equity premium puzzle.

An alternative approach to modeling the riskiness of stocks is to incorporate in the model spans of good years (high consumption growth) and spans of bad years (low consumption growth), with unpredictable switches between the two. Shmuel Kandel and Robert Stambaugh (1990) and Cecchetti, Lam, and Mark (1991) used this approach, but concluded that a high value of $\lambda$ was still needed to explain the historically observed equity premium. Although this richer process of underlying risk did not help explain the average rates of return on stocks and bills, Kandel and Stambaugh point out that it helps explain other statistical features of returns, such as their predictability.

Another way to enrich the model of risk is to relax the assumption that fluctuations in dividends are matched exactly by fluctuations in consumption. One approach, followed by Cecchetti, Lam, and Mark (1991) and Kandel and Stambaugh (1990 and 1991), is to account for the fact that stocks are levered claims on firms. Firms generally raise capital by issuing both stocks and bonds. Because firms must pay their obligations to bondholders before they can pay dividends to stockholders, leverage tends to increase the riskiness of a stock and would increase the equity premium in the CCAPM. However, even taking account of historically observed degrees of leverage, a high value of $\lambda$ is still needed to account for the

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historically observed value of the equity premium.

A more empirical approach to relaxing the assumption that fluctuations in dividends are matched exactly by fluctuations in consumption is simply to use historical data on dividends to measure dividend variability, and historical data on consumption to measure consumption variability. As pointed out by Cecchetti, Lam, and Mark (1991), dividends are much more variable than consumption.\(^{14}\) Using the actual variability of dividends in the CCAPI raises the equity premium predicted by the CCAPI by about 50 percent for any given value of \(A\).\(^{13}\)

The general conclusion is that richer models of underlying risk can raise the value of the equity premium predicted by the CCAPI. However, the CCAPI still predicts a value for the equity premium that is much lower than the actual historical average value, if we continue to use a coefficient of relative risk aversion less than or equal to 10.

**Differences Among Investors.** The research discussed so far has assumed that investors are identical in all respects. Like other assumptions used in economic models, this one was made for the sake of simplicity. The question is whether this assumption is responsible for the small predicted value of the equity premium in most applications of the CCAPI.

To get an idea of the differences among investors and their portfolios, N. Gregory Mankiw and Stephen Zeldes (1991) studied the asset holdings of 2998 families. They found a striking degree of variation in the portfolios held. In particular, 72.4 percent of the families in the survey held no stocks at all.\(^{16}\) Even among families that held more than \$100,000 in other liquid assets, only 48 percent held stock. This finding is important because, to determine the prices of assets, the CCAPI typically uses the covariance of stock returns and aggregate consumption per capita.

But with almost three-fourths of the families holding no stock at all, the covariance should be calculated using the consumption not of all the families but only of those that hold stocks. Having made this change, Mankiw and Zeldes find that the covariance of stock returns and consumption per family triples, reflecting the fact that, compared to nonstockholders, stockholders have more volatile consumption and their consumption is more closely related to stock returns. This tripling of the covariance of stock returns and consumption reduces by about two-thirds the value of \(A\) needed to account for the equity premium. This finding is appealing, but leaves us asking why so many consumers—especially wealthy consumers

\(^{14}\)If the growth rates of consumption and dividends are jointly identically and independently distributed, the equity premium is approximately proportional to A times Cov(consumption growth, dividend growth). Using consumption growth to measure dividend growth in the CCAPI, the equity premium is approximately proportional to A times Var(consumption growth). Using data from Cecchetti, Lam, and Mark, Cov(consumption growth, dividend growth) = 0.002053 and Var(consumption growth) = 0.001396. Therefore, using actual dividend growth increases the equity premium by about 47 percent because 0.002053 / 0.001396 is about 1.47 times as large as 0.001396.

\(^{16}\)For the purposes of this study, a family that held stocks in a pension fund but did not directly own stocks was considered a nonstockholding family. Mankiw and Zeldes argue that this treatment is appropriate because only 49 percent of the labor force had a pension fund, and only 31 percent of those people had defined-contribution (rather than defined-benefit) plans. Thus, only 16 percent of the labor force had defined-contribution plans. In defined-benefit plans, the stocks held by the pension fund are more appropriately regarded as being owned by the employing firms rather than the worker because the firm bears the risk of changes in the value of stocks.
with large amounts of liquid wealth—hold no stock.

A more fundamental question is why consumption behaves so differently for different groups of consumers. The CCAFM is based on the assumption that even though individuals face idiosyncratic risks that do not hit everyone in the economy, they can protect their consumption from such risks by various sorts of risk-sharing and insurance arrangements. For example, life insurance, disability insurance, fire insurance, and so on protect an individual’s consumption against various idiosyncratic risks. But problems such as the costs and difficulties of writing and enforcing various contracts prevent complete sharing of idiosyncratic risks. Theoretical studies have examined the impact of idiosyncratic risks on the equity premium, but these studies do not provide empirical evidence of the importance of these factors in accounting for the equity premium puzzle. Further research in this area is needed.

**Attitudes Toward Risk.** Investors’ attitudes toward risk are represented in economic models by utility functions that specify how much utility, or satisfaction, an investor gets for each possible level of consumption. The most commonly used version of the CCAFM is based on a particular utility function with two important features: (1) consumption in any year affects utility in that year only; and (2) the utility function has a constant coefficient of relative risk aversion, which implies that the share of the portfolio held in risky assets does not depend on how much wealth the investor has. Utility functions with these features are convenient, but have an important limitation: they do not distinguish an investor’s aversion to risk from his aversion to switching some consumption from one year to another year.

Kandel and Stambaugh (1991), Narayana Kocherlakota (1990), and Philippe Weil (1989) have investigated rates of return in the CCAFM using a more flexible utility function that distinguishes aversion to risk from aversion to substituting consumptions between different years. However, they all conclude that, even with this more flexible structure, a very high value of the coefficient of relative risk aversion is needed to account for the historical value of the equity premium.

Moreover, Kandel and Stambaugh (1991) have suggested that the search for a version of the CCAFM that can explain a large equity premium with a value for A of less than 10 is perhaps misdirected. They argue that the conventional view that A is small (less than 10) is based on an unconvincing body of evidence. Furthermore, they point out that for risks that represent a relatively small portion of total wealth, high values of A may be plausible. For example, to avoid a risky situation that involves either a 1 percent gain or 1 percent loss of wealth with equal probabilities, a person with A = 30 would be willing to pay an insurance premium of 0.15 percent of his wealth (15 percent of the amount at risk), which is not implausible. Because high values of A (around 30) may be plausible for small risks, the important issue for asset pricing considerations is the degree of risk aversion appropriate for the magnitude of the risks investors bear in their portfolios. The value of A is extremely important for the equity premium puzzle because the CCAFM will produce a high value of the equity premium if A is large.

Until this issue is resolved, Kandel and Stambaugh urge us not to rule out high values of A, if we continue to use utility functions that
have a constant coefficient of relative risk aversion. In light of the difference in plausible values of A for small and large risks, it may be
appropriate to use more general utility functions for which the coefficient of relative risk aversion is not constant. Future research may pursue this suggestion.

Another modification of the attitude toward risk is to assume that an investor cares about his level of consumption relative to a benchmark or accustomed level of consumption attained in the recent past. So far, studies have taken two approaches to modeling an accustomed level of consumption. In one approach, dubbed “catching up with the Joneses,” an investor cares about the level of his consumption relative to the accustomed national average level of consumption (modeled as the level of national consumption per capita in the previous year). In this case, what an investor needs to guard against is not a decline in his own consumption per se, but a decline in consumption relative to the national level of consumption per capita attained in the previous year. With the level of consumption per capita generally growing over time, stocks that have a risk of occasional negative returns appear very risky; investors would be willing to hold stocks only if they offer a large expected equity premium. Using this modification of the utility function in simulations of the CCAPM can produce average rates of return of 6.70 percent per year on stocks and 2.07 percent per year on bills, with a value for A equal to only 6.15

In the other approach to modeling an accustomed level of consumption—known as “habit formation”—an individual investor’s utility in any year depends on his level of consumption in that year compared to the level of his own consumption in the recent past.31 Like the “catching up with the Joneses” model, habit

formation makes investors more loath to hold risky assets that could earn negative net rates of return. Thus, stocks will have to offer a sizable equity premium for investors to be willing to hold them in their portfolios. Abel (1990) and George Constantinides (1990) have used habit formation in the CCAPM with low values of A to generate fairly realistic values for the equity premium.

CONCLUSION

Rather than discouraging use of the CCAPM, the equity premium puzzle has provided the impetus for new lines of research aimed at making the statistical predictions of the CCAPM conform more closely to the statistical behavior of actual rates of return. One line of research has focused on producing additional data on asset returns and characterizing the statistical behavior of the actual rates of return on stocks and bills. This line of research has produced useful new information about the statistical properties of asset returns over an extended period of time.

Another line of research has focused on modifications of the basic CCAPM. Some of the modifications, such as taking account of differences among investors and incorporating more general attitudes toward risk, seem to help account for part of the large historically observed value of the average equity premium. But accounting for the equity premium is only a first step in accounting for the statistical behavior of asset returns. A good model of asset returns should also account for other statistical properties, such as the variability or

31 Another modification of the attitude toward risk is studied by Nason (1988), who introduces a time-varying lower bound on consumption in the utility function. This formulation has some analytic similarities to “catching up with the Joneses” and habit formation, though it differs from these formulations.

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predictability of returns. In addition, a model that relates asset returns to consumption should be tested to see whether it is consistent with data on consumption by individuals and by the economy as a whole.

Some of the research discussed in this article, notably Cecchetti, Lam, and Mark (1990), Kandel and Stambaugh (1990, 1991), and Constantinides (1990), has already begun to examine other statistical properties of returns, but more remains to be studied.

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REFERENCES (continued)


